## GBGI9U07: multimedia document: description and automatic retrieval

## 1. Introduction, descriptors and correspondence

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## Outline

- Introduction
- Query by example versus search
- Descriptors
- Classification, fusion, post-processing ...
- Conclusion
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## Introduction

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## Multimedia Retrieval

- User need $\rightarrow$ retrieved documents
- Images, audio, video
- Retrieval of full documents or passages (e.g. shots)
- Search paradigms:
- Surrounding text $\rightarrow$ may be missing, inaccurate or incomplete
- Query by example $\rightarrow$ need for what you are precisely looking for
- Content based search (using keywords or concepts) $\rightarrow$ need for content-based indexing $\rightarrow$ "semantic gap problem"
- Combinations including feedback
- Need for specific interfaces


## The "semantic gap"

"... the lack of coincidence between the information that one can extract from the visual data and the interpretation that the same data have for a user in a given situation" [Smeulders et al., 2002].

## The "semantic gap" problem


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## "Signal" level

- Signal :
- Variable in time, in space and/or in other physical dimensions,
- Analog : physical phenomenon (pressure of an acoustic wave or distribution of light intensity) or its modeling by another one (electronic or chemical for example),
-Digital : same content but "discretized"
- of the value,
- of time,
- of space,
- and/or others (light frequency for example).


## "Signal" level

- Signal, examples :
- Sound (monophonic) : values sampled at 16 kHz on 16 bits (one temporal dimension, zero spatial dimensions),
- Still image (monochrome) : values sampled on a 2D grid on 8 bits (zero temporal dimension, two spatial dimensions; the spatial sampling frequency depends upon the sensor),
- Stereo sound, color image: multiplication of the channels (additional dimension),
- Video (image sequence): like still image fixe but additionally sampled in time (24-30 Hz; one temporal dimension, two spatial dimensions, one chromatic dimension),
- Images 3D (scanners), 3D sequences, ...


## "Signal" and "semantic" levels

- Semantics (opposed to signal) :
- "Abstract" concepts and relations,
- Symbolic representations (also signal),
- Successive levels of abstraction from the "signal / physical / concrete / objective" level to the "semantic / conceptual / symbolic / abstract / subjective" level,
- Gap between the signal and semantic levels ("red" versus "700-600 nm"),
- Somewhat artificial distinction,
- Intermediate levels difficult to understand,
- Search at the signal level, at the semantic level or with a combination of both.


## Query by example versus search

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## Query BY Example (QBE)


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## Content based indexing by supervised learning



## Example : the QBIC system

- Query By Image Content, IBM (stopped demo) http://wwwqुic.almaden.ibm.com/cgi-bin/photo-demo


## CBIG

Usage: 回: Get Info $\quad$ : Find Similar Color ©: Find Similar Colors $\boxed{\square}$ : Find Similar Layout $\boldsymbol{\top}$ : Find Similar Texture


## Content-based search

- Aspects :
- Signal : arrays of numbers ("low level"),
- Semantic : concepts or keywords ("high level").
- Search :
- Semantic $\rightarrow$ semantic : classical for text,
- Semantic $\rightarrow$ signal : images corresponding to a concept ?
- Signal $\rightarrow$ signal : image containing a part of another image ?
- Signal $\rightarrow$ semantic : concepts associated to an image ?
- Approaches:
- Bottom-up : signal $\rightarrow$ semantic,
- Top-down : semantic $\rightarrow$ signal,
- Combination of both.


## Document representation

- Compression : encoding and decoding
- Indexing : characterization of the contents

JPEG<br>GIF<br>PNG<br>MJPEG<br>DV<br>MPEG-1<br>MPEG-2<br>MPEG-4



Documents


Indexing


Representation

Retrieval

Reference

## Problems

- Choice of a representation model,
- Indexing method and index organization,
- Choice and implementation of the search engine,
- Very high data volume,
- Need for manual intervention.


## Representation models

- Semantic level:
- keywords, word groups, concepts (thesaurus),
- Conceptual graphs (concepts and relations),
- Signal level:
- Feature vectors,
- Sets of interest points,
- Intermediate level:
- Transcription of the audio track,
- Sets of key frames,
- Mixed and structured representations, levels of detail,
- Application domain specificities,
- Standards (MPEG 7).
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## Indexing methods and index organization

- Build representations from document contents,
- Extract features for each document or document part:
- Signal level: automatic processing,
- Semantic level : more complex, manual to automatic.
- Globally organize the features fo the search:
- Sort, classify, weight, tabulate, format, ...
- Application domain specificities,
- Problem of the quality versus cost compromise.
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## Choice and implementation of the search engine

- Search for the "best correspondence" between a query and the documents,
- Semantic $\rightarrow$ semantic:
- Logical, vector space and probabilistic models,
- Keywords, word groups, concepts, conceptual graphs, ...
- Signal $\rightarrow$ signal :
- Color, texture, points of interest, ...
- Images, imagettes, pieces of image, sketches, ...
- Semantic $\rightarrow$ signal :
- Correspondence evaluated during the indexing phase (in general).
- Search with mixed queries.
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## Descriptors

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## Descriptors

- Engineered descriptors
- Color
- Texture
- Shape
- Points of interest
- Motion
- Semantic
- Local versus global
- ...
- Learned descriptors
- Deep learning
- Auto encoders
- ...
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## Histograms - general form

- A fixed set of disjoint categories (or bins), numbered from 1 to $K$.
- A set of observations that fall into these categories
- The histogram is the vector of $K$ values $h[k]$ with $h[k]$ corresponding to the number of observations that fell into the category $k$.
- By default, the $h[k]$ are integer values but they can also be turned into real numbers and normalized so that the $h$ vector length is equal to 1 considering either the $L_{1}$ or $L_{2}$ norm
- Histograms can be computed for several sets of observations using the same set of categories producing one vector of values for each input set


## Histograms - text example

- A vector of term frequencies (tf) is an histogram
- The categories are the index terms
- The observations are the terms in the documents that are also in the index
- A tf.idf representation corresponds to a weighting of the bins, less relevant in multimedia since histograms bins are more symmetrical by construction (e.g. built by Kmeans partitioning)


## Image intensity histogram

- The set of categories are the possible intensity values with 8 -bit coding, ranging from 0 (black) to 255 (white) or ranges of these intensity values


256-bin

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## Image color histogram

- The set of categories are ranges of possible color values
- A common choice is a per component decomposition resulting in a set of parallelepipeds


Representations with the parallelepipeds' center colors:


$$
5 \times 5 \times 5 \text {-bin }
$$

125-bin


$$
\begin{gathered}
4 \times 4 \times 4 \text {-bin } \\
64 \text {-bin }
\end{gathered}
$$

- Any color space can be chosen (YUV, HSV, LAB ...)
- Any number of bins can be chosen for each dimension
- The partition does not need to be in parallelepipeds
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## Image color histogram

- The set of categories are ranges of possible color values

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## Image histograms

- Rather invariant to image size if normalized to unit vector length with $L_{1}$ or $L_{2}$ norm
- Rather invariant to content displacements or symmetries
- NOT invariant to illuminations changes, gain and offset normalization may be needed
- Histograms are distributions, better compared using a $\chi 2$ distance that Euclidean one:

$$
d(x, y)=\sum_{i} \frac{\left(x_{i}-y_{i}\right)^{2}}{x_{i}+y_{i}}
$$

- Earth Mover Distance (EMD) can be even better
- Alternatively, taking the square root of the histogram elements can make the Euclidean distance suitable


## Image histograms

- Can be computed on the whole image,
- Can be computed by blocks:
-One (mono or multidimensional) histogram per image block,
-The descriptor is the concatenation of the histograms of the different blocks.
-Typically : $4 \times 4$ complementary blocks but non symmetrical and/or non complementary choices are also possible. For instance: $2 \times 2+1 \times 3+1 \times 1$
- Size problem $\rightarrow$ only a few bins per dimension or a lot of bins in total


## Fuzzy histograms

- Objective: smooth the quantization effect associated to the large size of bins (typically $4 \times 4 \times 4$ for RGB).
- Principle: split the accumulated value into two adjacent bins according to the distance to the bin centers.


## Color spaces

- Linear:
-RGB: Red, green, blue
- YUV: Luminance, chrominance (L - red, L - blue)
- Non linear:
- HSV: Hue, Saturation, Value
- LAB: Luminance, "blue - yellow", "green - red"


## Color moments

- Moments (color distribution global statistics)
-Means
-Covariances
-Third order moments
-Can be combined with image coordinates
-Fast and easy to compute and compact representation but not very accurate


## Color moments

- Means: $m \mathrm{~m}=(\Sigma \mathrm{R}) / \mathrm{N}, \quad \mathrm{mG}=(\Sigma \mathrm{G}) / \mathrm{N}, \quad \mathrm{mB}=(\Sigma \mathrm{B}) / \mathrm{N})$
- Means + variances: + covariances: $m R R=\left(\Sigma(\mathrm{R}-\mathrm{mR})^{2}\right) / \mathrm{N}, \quad \mathrm{mGB}=(\Sigma(\mathrm{G}-\mathrm{mG})(\mathrm{B}-\mathrm{mB})) / \mathrm{N}$,
- Higher order moments: $m R G B=(\Sigma(R-m R)(G-m G)(B-m B)) / N, m R R R$, mRGG, ...
- Moments associated to spatial components: $m R X=(\Sigma(R-m R)(X-m X)) / N, \quad m R G X, m B X Y, \ldots$
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## Image normalization

- Objective : to become more robust against illumination changes before extracting the descriptors.
- Gain and offset normalization: enforce a mean and a variance value by applying the same affine transform to all the color components, non-linear variants.
- Histogram equalization: enforce an as flat as possible histogram for the luminance component by applying the same increasing and continuous function to all the color components.
- Color normalization: enforce a normalization which is similar to the one performed by the human visual: "global" and highly non linear.


## Correspondence functions for color

- Vectors of moments:
- Euclidean distance : search for exact similarity,
- Angle between vectors : search for similarity with robustness to illumination changes,
- Histograms:
- Euclidean or $\chi^{2}$ distance: search for exact similarity,
- Robustness to illumination changes can only be obtained by an intensity normalization pre-processing,
- Earth-mover distance: compute the cost for transforming one histogram into another by giving a flat penalty for passing from one bin to another
- Histograms by blocks : sum of the smaller block to block distances only (typically 8 out of 16): permits a search with only a portion of an image,
- Correlograms:
- Euclidean or $\chi^{2}$ distance, with or without intensity normalization.
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## Texture descriptors

- Computed on the luminance component only
- Rather fuzzy concept,
- Frequential composition or local variability,
- Fourier transforms,
- Gabor filters,
- Neuronal filters,
- Cooccurrence matrices,
- Many possible combination,
- Feature vector,
- Associated correspondence functions,
- Normalization possible.
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## 1D discrete convolution

Mathematical definition:

- $f$ and $g$ : functions from $\mathbb{Z}$ to $\mathbb{R}$ (or to $\mathbb{C}$ )

$$
(f * g)(n)=\sum_{m \in \mathbb{Z}} f(m) g(n-m)=\sum_{m \in \mathbb{Z}} f(n-m) g(m)
$$

- Infinite sums must be convergent
- In practice: $f$ and $g$ are defined on bounded regions $\rightarrow$ padding (usually with zeroes) $\rightarrow$ "side effects"


## 1D discrete convolution

Signal processing:

- Application of a 1D convolution kernel $K$ to a 1D input signal $I$ for producing an output signal $O=K * I$ with $O(n)=\sum_{m \in W} K(m) I(n-m)$
- $m$ : within a finite (and usually centered) window $W$ around the current location ( $n$ )
- Properties: linear (relatively to $I$ ), "local" and translation invariant
- The convolution product is commutative and associative: the sequential application of several kernels is the same as a single application of their product


## 1D discrete convolution

Signal processing:

- Application of a1D convolution kernel $K$ to a 1D input signal $I$

(0,1,2,3,4,5)



## 1D discrete convolution



## 1D discrete convolution



## 1D discrete convolution



## 1D discrete convolution



## 1D discrete convolution



Side effects (continuity padding)

## 1D discrete convolution



## 1D discrete convolution



## 1D discrete convolution

## Examples:

- Derivative: $D(m)=(\delta(m+1)-\delta(m-1)) / 2$ $(D(m)=+1$ if $m=-1,-1$ if $m=+1,0$ otherwise) i.e.: $O(n)=(I(n+1)-I(n-1)) / 2$
- Average on a sliding window (basic smoothing): $A(m)=\frac{1}{2 w+1}$ if $|m| \leq w, 0$ otherwise. Window size is $2 w+1$.
- Gaussian smoothing: $G_{\sigma}(m)=\frac{1}{\sqrt{2 \pi} \sigma} e^{-\frac{m^{2}}{2 \sigma^{2}}}$ practical extension: 3-4б


## 1D discrete convolution

Examples (all kernels are centered):

- Derivative: $D=\frac{1}{2} \times$| 1 | 0 | -1 |
| :--- | :--- | :--- |
- Sliding average: $A_{2}=\frac{1}{5} \times$| 1 | 1 | 1 | 1 | 1 |
| :--- | :--- | :--- | :--- | :--- |
- Binomial filter (discrete and bounded Gaussian filter)

$$
\begin{aligned}
& B_{w}(m)=\frac{C_{2 w}^{m+w}}{2^{2 w}}=\frac{l}{2^{2 w}(w-m)!(w+m)!} \\
& B_{1}=\frac{1}{4} \times \begin{array}{|l|l|l|l|l|}
\hline \mathbf{1} & \mathbf{2} & \mathbf{1} \\
\hline
\end{array} \\
& B_{2}=\frac{1}{16} \times \begin{array}{|l|l|l|l|l|l|}
\hline \mathbf{1} & \mathbf{4} & \mathbf{6} & \mathbf{4} & \mathbf{1} \\
\hline
\end{array} \\
& B_{3}=\frac{1}{64} \times \begin{array}{|l|l|l|l|l|l|l|}
\hline \mathbf{1} & \mathbf{6} & \mathbf{1 5} & \mathbf{2 0} & \mathbf{1 5} & \mathbf{6} & \mathbf{1} \\
\hline
\end{array}
\end{aligned}
$$

## 2D (image) convolution

- $O(i, j)=(K * I)(i, j)=\sum_{(m, n)} K(m, n) I(i-m, j-n)$
- $m$ and $n$ : within a window around the current location, corresponding to the filter size
- $K(m, n)$ : convolution kernel, usually bounded
- Linear, "local" and translation invariant
- Side effects


## Classical image convolution (2D to 2D)


$3 \times 3$ convolution, no stride, half padding
Animation from https://github.com/vdumoulin/conv_arithmetic/

## Classical image convolution (2D to 2D)


$3 \times 3$ convolution, no stride, no padding
Animation from https://github.com/vdumoulin/conv_arithmetic/

## Classical image convolution (2D to 2D)


$3 \times 3$ convolution, no stride, full padding
Animation from https://github.com/vdumoulin/conv_arithmetic/

## 2D discrete convolution

Examples, partial derivatives (all kernels are centered):

- $\partial / \partial x=\frac{1}{2} \times$| 0 | 0 | 0 |
| :---: | :---: | :---: |
| 1 | 0 | -1 |
| 0 | 0 | 0 |$=\frac{1}{2} \times$| 1 | 0 | -1 |
| :--- | :--- | :--- |
- $\partial / \partial y=\frac{1}{2} \times$| 0 | 1 | 0 |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 0 | -1 | 0 |$=\frac{1}{2} \times$| 1 |
| :---: |
| 0 |
| -1 |


## 2D discrete convolution

Examples, partial derivatives (all kernels are centered):


## 2D discrete convolution

Partial derivatives, smoothed versions:

- $\partial / \partial x=\frac{1}{2} \times$| 1 | 0 | -1 |
| :--- | :--- | :--- |$* \frac{1}{4} \times$| 1 |
| :--- |
| 2 |
| 1 |$=\frac{1}{8} \times$| 1 | 0 | -1 |
| :---: | :---: | :---: |
| 2 | 0 | -2 |
| 1 | 0 | -1 |
- $\partial / \partial y=\frac{1}{2} \times$| 1 |
| :---: |
| 0 |
| -1 |$* \frac{1}{4} \times$| 1 | 2 | 1 |
| :---: | :---: | :---: |$=\frac{1}{8} \times$| 1 | 2 | 1 |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| -1 | -2 | -1 |


## 2D discrete convolution

Partial derivatives, smoothed versions:


## Gabor filter

- Circular Gabor filter:

$$
G_{\square \theta}(m, n)=\frac{1}{2 \pi \sigma^{2}} \cdot e^{-\frac{m^{2}+n^{2}}{2 \sigma^{2}}} \cdot e^{2 \pi i \frac{m \cdot \cos \theta+n \cdot \sin \theta}{\lambda}}
$$



Gaussian:

- Locality
- Side effect
- Filter width

Wave:

- Wave length
- Orientation


## Gabor transforms

(Circular) Gabor filter of direction $\theta$, of wavelength $\lambda$ and of extension $\sigma$ :

$$
g(\sigma, \theta, \lambda, I, i, j)=\frac{1}{2 \pi \sigma^{2}} \sum_{k, l} e^{-\left(\frac{k^{2}+l^{2}}{2 \sigma^{2}}\right)} \cdot e^{2 \pi \mathrm{i}\left(\frac{k \cdot \cos \theta+\lambda \cdot \sin \theta}{\lambda}\right)} \cdot I(i+k, j+l)
$$

Energy of the image through this filter:

$$
E_{g}(\sigma, \theta, \lambda, I)^{2}=\frac{1}{N} \sum_{i, j}|g(\sigma, \theta, \lambda, I, i, j)|^{2}
$$

Set of convolutional (linear) transform followed by a non-linear transformation (module) and a global pooling (average) : specific case of CNN layer.

## Gabor transforms

"Separable" formulation:

$$
\begin{gathered}
g(\sigma, \theta, \lambda, I, i, j)=\sum_{l} \frac{e^{-\left(\frac{l^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} \cdot e^{2 \pi \mathrm{i}\left(\frac{l \cdot \sin \theta}{\lambda}\right)} \cdot\left(\sum_{k} \frac{e^{-\left(\frac{k^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} \cdot e^{2 \pi \mathrm{i}\left(\frac{(\cdot \cos \theta}{\lambda}\right)} \cdot I(i+k, j+l)\right) \\
h(\sigma, \theta, \lambda, I, i, j)=\sum_{k} \frac{e^{-\left(\frac{k^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} \cdot e^{2 \pi \mathrm{i}\left(\frac{k \cdot c o s \theta}{\lambda}\right)} \cdot I(i+k, j)=H(i, j) \\
g(\sigma, \theta, \lambda, I, i, j)=\sum_{l} \frac{e^{-\left(\frac{l^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} e^{2 \pi \mathrm{i}\left(\frac{l \cdot \sin \theta}{\lambda}\right)} \cdot h(\sigma, \theta, \lambda, I, i, j+l)=G(i, j)
\end{gathered}
$$

## Gabor transforms

Linear combination coefficients:

$$
\begin{aligned}
c(k) & =\frac{e^{-\left(\frac{k^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} \cdot\left(\cos \left(\frac{2 \pi k \cdot \cos \theta}{\lambda}\right)+\mathbf{i} \cdot \sin \left(\frac{2 \pi k \cdot \cos \theta}{\lambda}\right)\right) \\
d(l) & =\frac{e^{-\left(\frac{l^{2}}{2 \sigma^{2}}\right)}}{\sqrt{2 \pi} \sigma} \cdot\left(\cos \left(\frac{2 \pi l \cdot \sin \theta}{\lambda}\right)+\mathbf{i} \cdot \sin \left(\frac{2 \pi l \cdot \sin \theta}{\lambda}\right)\right)
\end{aligned}
$$

## Gabor transforms

Simplified expressions:

$$
\begin{aligned}
H(i, j) & =\sum_{k} c(k) \cdot I(i+k, j) \\
G(i, j) & =\sum_{l} d(l) \cdot H(i, j+l) \\
E^{2} & =\frac{1}{N} \sum_{i, j}|G(i, j)|^{2}
\end{aligned}
$$

## Gabor transforms

Elliptic:

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## Filtres de Gabor

Example of elliptic filters with 8 orientations and 4 scales

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## Gabor filters in Fourier space

Elliptic filters with 6 orientations and 4 scales in the frequential domain (Fourier space)

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## Gabor transforms

- Circular:
- scale $\lambda$, angle $\theta$, variance $\sigma$,
$-\sigma$ multiple of $\lambda$, typically $: \sigma=1.25 \lambda$,
("same number" of wavelength whatever the $\lambda$ value)
- Elliptic:
- scale $\lambda$, angle $\theta$, variances $\sigma_{\lambda}$ and $\sigma_{\theta}$,
$-\sigma_{\lambda}$ and $\sigma_{\theta}$ multiples of $\lambda$, typically : $\sigma_{\lambda}=0.8 \lambda$ et $\sigma_{\theta}=1.6 \lambda$,
- 2 independent variables:
- scale $\lambda$ : $N$ values (typically 4 to 8 ) on a logarithmic scale (typical ratio of $\sqrt{ } 2$ to 2 )
- angle $\theta$ : $P$ values (typically 8),
- N.P elements in the descriptor,


## Correspondence Functions for Gabor transforms

- Euclidean Distance : searching for identities,
- Angle between vectors : searching for similarities robust to illumination changes,


## Descriptors of points of interest

- "High curvature" points or "corners",
- Singular" points of the I[i][j] surface,
- Extracted using various filters:
- Computation of the spatial derivatives at a given scale,
- Convolution with derivatives of Gaussians,
- Harris-Laplace detector.
- Construction of invariants by an appropriate combination of these various derivatives,
- Each point is selected and then represented by the set of values of these invariants,
- The set of selected points of interest is topologically organized (relations between neighbor points),
- The structure is irregular and the size of the description depends upon the image contents,
- Descriptions are large.
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## Descriptors of points of interest

- SIFT descritptor: Histogram of gradient direction: 8 bins times $4 \times 4$ blocks in a neighborhood of the point.

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## Local versus global descriptors

- Global descriptors: single vector for a whole image
- Local descriptors: one vector for each pixel, image patch, image block shot 3D patch ... e.g. SIFT or STIP
- Need for a single vector of fixed length far any image and with comparable components across images
- Aggregation of local descriptors $\rightarrow$ global descriptor
- Homogeneous with the local descriptor:
- max or average pooling
- Heterogeneous with the local descriptor:
- Histogramming according to clusters in the local descriptor space [Sivic, 2003][Cusrka, 2004]
- Gaussian Mixture Models (GMM)
- Fisher Vectors (FV) [Perronnin, 2006], Vectors of Locally Aggregated Descriptors (VLAD) [Jégou, 2010] or Tensors (VLAT) [Gosselin, 2011], Supervectors
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## Aggregation of local descriptors

- Histogramming according to clusters in the local descriptor space:
- Clustering: partitioning of the descriptor space according to training data:
- k-means or equivalent method
- each cluster is represented by its centroid
- Mapping: associating a local descriptor to a cluster:
- getting a cluster number for each local descriptor
- number of the nearest centroid vector
- Histogramming: counting the local descriptors in each cluster for a given image:
- one histogram per image


## Clustering

- Given a set $\left(x_{i}\right)$ of $N$ data points in a metric space
- Find a set $\left(c_{j}\right)$ of $K$ centers
- Minimizing the representation square error:

$$
E=\sum_{i}\left(\min _{j}\left(d\left(x_{i}, c_{j}\right)^{2}\right)\right)
$$

- Direct search not possible
- Use heuristics for finding good local minima
- Cluster $j=$ subset (part) of the data space which is closest to center $c_{j}$ than to any other center
- The set of clusters is a partition of the data space
- This partition is adapted to the training data
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## K-means Clustering

- Given a set $\left(x_{i}\right)$ of $N$ data points in a metric space
- Randomly select a set $\left(c_{j}\right)$ of $K$ centers
- Repeat until convergence (no change in centers):
- for each $x_{i}$ data point, $i=1 \ldots N$ :
- find the nearest center $\quad c_{j}: j=\arg \min d\left(x_{i j}, c_{k}\right)$
- assign the $x_{i}$ data point to the cluster $j \quad x_{i} \rightarrow c_{j}$
- for each cluster, $j=1 \ldots K$ :
- set the new center $c_{j}$ as the mean of all $x_{i}$ data point previously assigned to the cluster $j$ : or to a random value if no data point is assigned

$$
c_{j}=\frac{\sum_{x_{i} \rightarrow c_{j}} x_{i}}{\sum_{x_{i} \rightarrow c_{j}} 1}
$$

- Complexity: O(\#iterations $\times$ \#clusters $\times$ \#points $\times$ \#dimensions)
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## K-means Clustering

- K-means is relatively fast and efficient compared to alternate and more complex methods
- The final result depends upon the choice of the initial centers; it is always possible to run it many times with different initial conditions and select the one obtaining the smallest representation error
- Tends do produce clusters of comparable size
- Convergence is guaranteed but it may take a large number of iterations
- For practical applications, a full convergence is not necessary and does not make a big difference
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## Hierarchical K-means Clustering

- Hierarchical K means may be faster (both for the clustering and the mapping) but less accurate
- The hierarchical structure of the set of clusters may be useful for some applications
- Two main strategies:
- Recursively split all the clusters into a (small) fixed number of subclusters (e.g. recursive dichotomy) starting with a single cluster ( $\rightarrow$ regular n -ary tree)
- Recursively split in two parts only the biggest cluster into subclusters ( $\rightarrow$ irregular binary tree)
- Hierarchical mapping: recursive search of the closest center from the coarsest to the finest grain.
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## Correspondence functions for points of interest

- Generally very complex functions,
- Relaxation methods:
- Randomly choose a point in the description of the query image,
- Compare the neighborhood of this point to all the neighborhoods of all the points of the candidate document,
- Amongst those that are "close" in the sense of the spatial relations and the values of the associated attributes, do a complementary search to see if the neighbor points are also "close" in the same sense,
- Propagate the correspondence between "close" points by following the point topologies in the query and candidate images,
- Find the best possible global correspondence respecting these topologies et preserving close characteristics for the in correspondence,
- Globally evaluate (quantify) the quality of the correspondence.


## Correspondence functions for points of interest

- Very costly method both for representation volume and computation time for the correspondence function,
- But very accurate and selective,
- Allows for retrieving an image from a portion of it by searching for a partial correspondence,
- Can be made robust to rotations by choosing appropriate invariants,
- Can be made robust to scale transforms by using multiscale representations (even more costly)
- Usable only on small to medium image collections (~100010,000 images)
- Recent progress: up to millions of images.
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## Correspondence functions for points of interest



Example of an image pair involving a large scale change due to the use of a zoom. The scale factor between the images is 6 . The common portion represents less than $17 \%$ of the image.
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## Use of several types of descriptors

- Several types of descriptors : choice according to the target application or to the query type,
- Several correspondence function for each type of descriptor : choice according to the target application or to the target query type (invariances that are desired or not for instance),
- Combination of the descriptions,
- Combination of the correspondence functions,
- Combination with descriptions from the semantic level.


## Query BY Example (QBE)


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## Content based indexing by supervised learning



## Common processing, single descriptor



Scores

Query,
search collection, training collection, test collection ...

Color, texture, bag of SIFTs ...

Correspondence function, train / predict

Similarity measure, probability of presence

## Common processing, multiple descriptors, single decision (early fusion)


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## Common processing, multiple descriptors, multiple decision (late fusion)


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## Fusion of representations (early)

- For all vector description (of fixed size), whatever their origin,
- Possibility to concatenate the various descriptors in a unique mixed descriptor $\rightarrow$ normalization problem,
- Possibility to reduce la dimension of the resulting vector (and/or of each original vector) in order to keep only the most relevant information:
- Principal Component Analysis,
- Neural networks,
- Learning is needed (representative data and process).
- Less information, faster once learning is done,
- Euclidean distance on the shortened vector.
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## Fusion of the correspondence functions (late)

- Each correspondence function generally produces a quantitative value that estimate a similarity,
- It is always possible to come to the case in which the values are between 0 and 1 and represent a relevance,
- In order to fuse the results from several functions, we may use :
- A weighted sum,
- A weighted product (weighted sum on the logarithms),
- The minimum value,
- A classifier (SVM, neural network, ...)
- Problem for the choice of the weights and/or for the classifier training.
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## Computation of the relevance

- Euclidean distance, angle between vectors,
- Comparison between a query vector to all the vectors in the database (no pre-selection),
- "Small" number of dimensions ( < 10) : clustering techniques hierarchical search,
- "Medium" number of dimensions ( $\sim 10+$ ) : methods based on space partitioning,
- "Large" number of dimensions( >> 10 ) : no known method faster that a full linear scan,
- Reduction of the number of dimensions by Principal Component Analysis.
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## Principal Component Analysis 1

- "Natural" data contain redundancies:
- Neighbor pixels' values are correlated
- Political opinions and age of people are correlated
- Weight and size of objects are correlated
-...
- Principal Component Analysis aims at
- Identify and characterize redundancies in data
- Transform data for removing and reducing redundancies and possibly noise
- "Ordinary or classical" PCA operates in the context of linear algebra (non linear variants also exist)


## Principal Component Analysis 2

- Redundancies are identified as correlations
- Correlation is measured by covariance
- Considering a set of samples $\left\{\left(x_{i}, y_{i}\right), i \in\{1 \ldots N\}\right.$, covariance is defined as:

$$
\operatorname{cov}(\boldsymbol{x}, \boldsymbol{y})=\frac{1}{N} \sum_{i=1}^{i=N}\left(x_{i}-\overline{\boldsymbol{x}}\right)\left(y_{i}-\overline{\boldsymbol{y}}\right) \quad \text { with: } \quad \overline{\boldsymbol{x}}=\frac{1}{N} \sum_{i=1}^{i=N} x_{i}
$$

- Correlation is defined as:

$$
\mathrm{r}=\frac{\operatorname{cov}(x, y)}{\sqrt{\operatorname{cov}(x, x) \operatorname{cov}(y, y)}}
$$

## Principal Component Analysis 3

- Examples: no correlation (normal distributions)

$$
\begin{aligned}
& \operatorname{cov}(x, x)=2500 \\
& \operatorname{cov}(x, y)=0 \\
& \operatorname{cov}(y, y)=2500 \\
& r=0
\end{aligned}
$$

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## Principal Component Analysis 4

- Examples: correlation (normal distributions)

$$
\begin{aligned}
& \operatorname{cov}(\mathrm{x}, \mathrm{x})=1800 \\
& \operatorname{cov}(\mathrm{x}, \mathrm{y})=1350 \\
& \operatorname{cov}(\mathrm{y}, \mathrm{y})=1800 \\
& \mathrm{r}=+0.75
\end{aligned}
$$

$$
\begin{aligned}
& \operatorname{cov}(\mathrm{x}, \mathrm{x})=1800 \\
& \operatorname{cov}(\mathrm{x}, \mathrm{y})=-1350 \\
& \operatorname{cov}(\mathrm{y}, \mathrm{y})=1800 \\
& \mathrm{r}=-0.75
\end{aligned}
$$

$$
\operatorname{cov}(x, x)=2500
$$

$$
\operatorname{cov}(x, y)=1470
$$

$$
\operatorname{cov}(y, y)=900
$$

$$
r=0.98
$$

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## Principal Component Analysis 5

- Covariance matrix:
$\Sigma=\left(\begin{array}{ll}\operatorname{cov}(x, x) & \operatorname{cov}(x, y) \\ \operatorname{cov}(y, x) & \operatorname{cov}(y, y)\end{array}\right)$
- Properties:
$-\Sigma$ is symmetric and positive $\rightarrow$ diagonalizable
$-\exists$ rotation matrix $R$ so that $R^{-1} \Sigma R$ is diagonal
- If the rotation $R$ is applied to the data:
- $\Sigma$ becomes diagonal
- r becomes 0
- the $x$ and $y$ components becomes decorrelated
- redundancy is removed
- Independent components can be sorted according to their variance (square root of the diagonal term)
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## Principal Component Analysis 6

- Rotation (and translation) of the data

$$
\begin{aligned}
& \operatorname{cov}(\mathrm{x}, \mathrm{x})=2500 \\
& \operatorname{cov}(\mathrm{x}, \mathrm{y})=1470 \\
& \operatorname{cov}(\mathrm{y}, \mathrm{y})=900 \\
& \mathrm{r}=0.98
\end{aligned}
$$

$$
\begin{aligned}
& \operatorname{cov}(x, x)=3364 \\
& \operatorname{cov}(x, y)=0 \\
& \operatorname{cov}(y, y)=49 \\
& r=0
\end{aligned}
$$


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## Principal Component Analysis 7

- Generalization from sets of two-dimensional samples $\left\{\left(x_{i}, y_{i}\right), i \in\{1 \ldots N\}\right\}$ to sets of $D$-dimensional samples $\left\{\left(x_{i 1}, x_{i 2} \quad \ldots x_{i D}\right), i \in\{1 \ldots N\}\right\}$
$\Sigma_{\boldsymbol{j} \boldsymbol{k}}=\operatorname{cov}\left(\boldsymbol{x}_{\boldsymbol{j}}, \boldsymbol{x}_{. \boldsymbol{k}}\right)=\frac{\mathbf{1}}{\boldsymbol{N}} \sum_{i=1}^{\boldsymbol{i}=\boldsymbol{N}}\left(x_{i j}-\overline{\boldsymbol{x}_{\cdot}}\right)\left(x_{i k}-\overline{\boldsymbol{x}_{. \boldsymbol{k}}}\right)$
- $\Sigma$ is a $D \times D$ symmetric and positive matrix that can be diagonalized as $R^{-1} \Sigma R$
- Data can be rotated and centered accordingly into decorrelated components of decreasing variance
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## Principal Component Analysis 8

- With real high-dimensional sets of samples, the variance of the decorrelated components decreases very rapidly
- If correlation is high in the data, many of the last components have very small variances
- Dropping the components with very small variance does not significantly change the results
- Dropping components whose variance is smaller than the level of noise even improve performance
- Dropping components is a linear projection
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## Principal Component Analysis 9

- PCA summary:
- Translation to center of data (removing mean vector)
- Rotation to the principal axes (from covariance matrix)
- Projection on the "big variance" axes (dropping of small variance components)
- PCA (almost) preserve the Euclidean distance
- Translation and rotation are isometries: they preserve Euclidean distance
- Projection dropping only small variance axes is close to an isometry: Euclidean distance is almost preserved
- Real data do not follow normal distributions but do exhibit significant correlations anyway
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## User interface

- Classical interface for the part of the query given at the semantic level (e.g. text input for keywords),
- Plus possibility to define a query at the signal level:
- Query by example : one or several images or video segments, initially given or selected during relevance feedback,
- Library of signal elements : colors, textures, shapes (that could be entered as sketches),
- Possibility to define a relative importance for the various signal (or semantic) features available,
- Possibility to define a fusion method for the correspondence functions (sum, product, min, ...),
- The system can also make these choices by analysis of the relevance feedback,
- Link between signal and semantics.
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## Search at the signal level: conclusion

- Representation by different types of descriptors and evaluation of relevance by various functions,
- A single type: results from poor to average,
- Several types simultaneously: results from average to good with possible domain adaptation
- Possibility to adjust the compromise quality performance - general - size of the database
- Performance limited by the "analog" (not symbolic) aspect of representations.
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